

# UNCERTAINTIES IN PRODUCTS DERIVED FROM RADAR

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Uncertainty in Radar Retrievals, Model Parameterizations, Assimilated Data  
and In-situ Observations: Implications for the Predictability of Weather  
October 31 – November 2, 2018, Norman

## **Layout of the talk**

- **Polarimetric microphysical retrievals in rain**
- **Polarimetric microphysical retrievals in ice / snow**
- **Multifrequency polarimetric radar retrievals**

## **Two possible ways to optimize microphysical parameterization of NWP models**

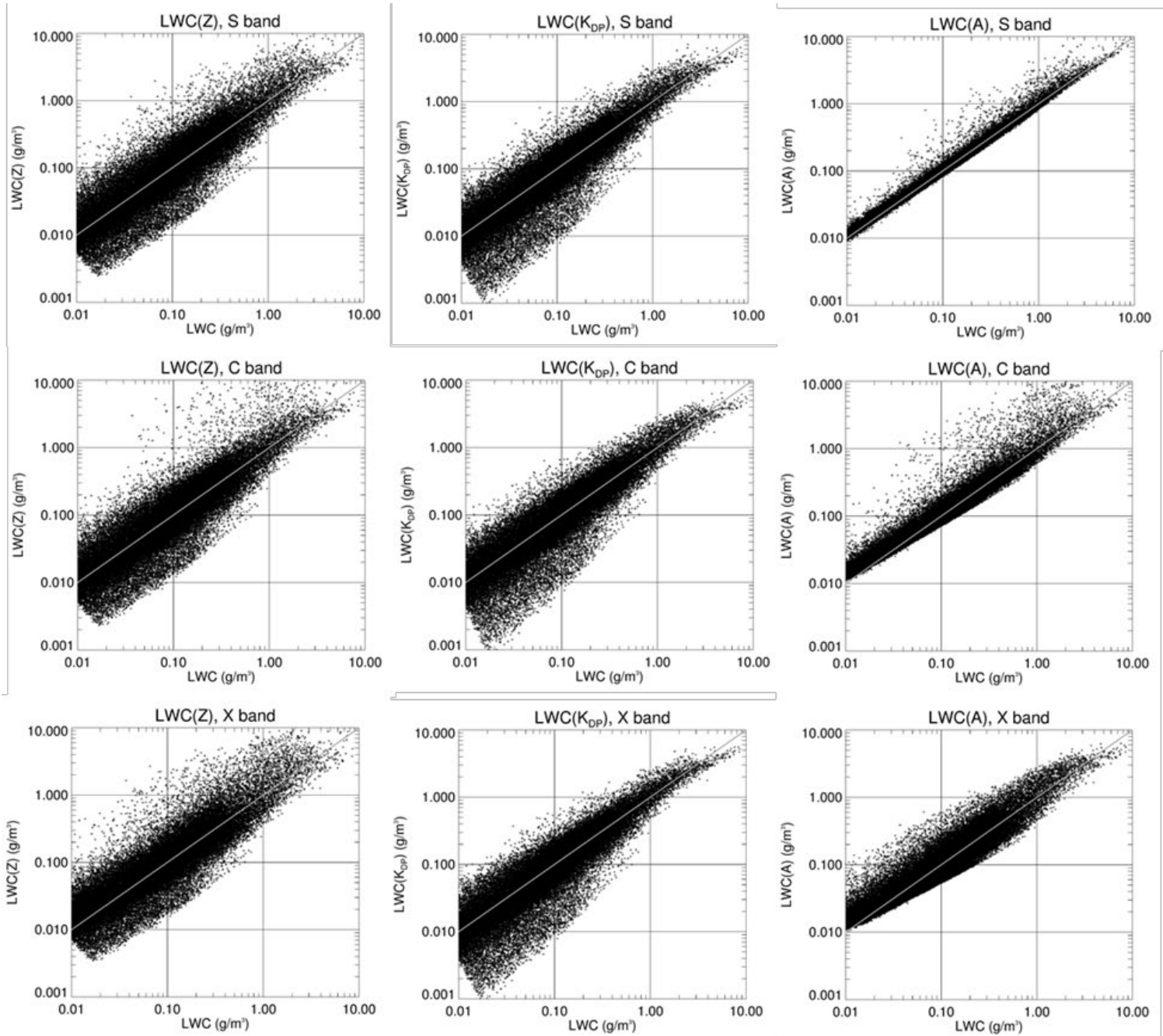
- **Radar microphysical retrievals**
- **Forward radar operators**

## **Two sources of errors in radar microphysical retrievals**

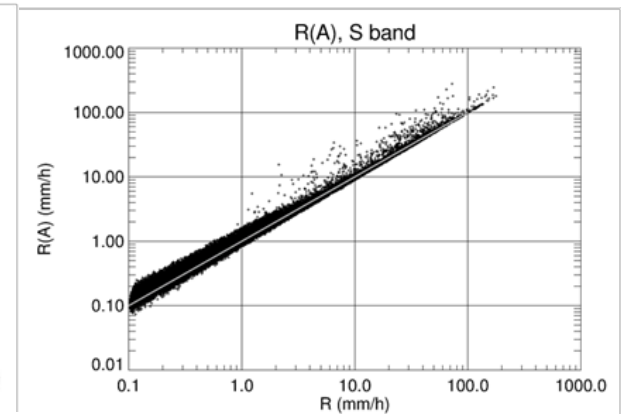
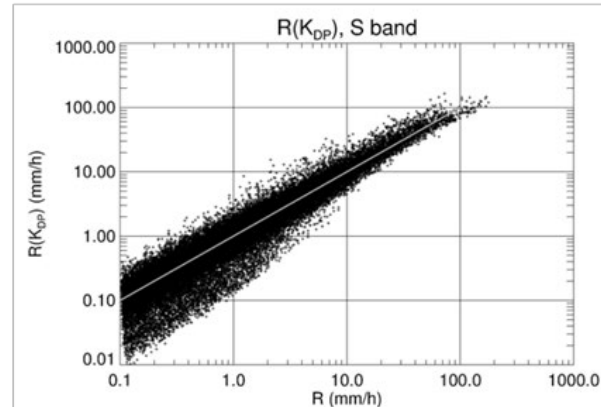
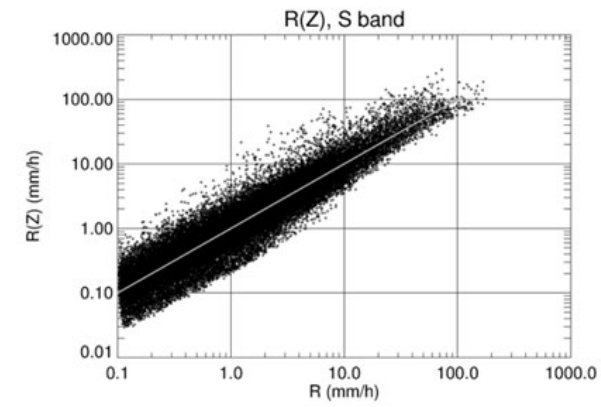
- **Errors due to natural variability of microphysical properties of hydrometeors**
- **Radar measurement errors**

# **Polarimetric microphysical retrievals in rain**

# Estimation of liquid water content (LWC)

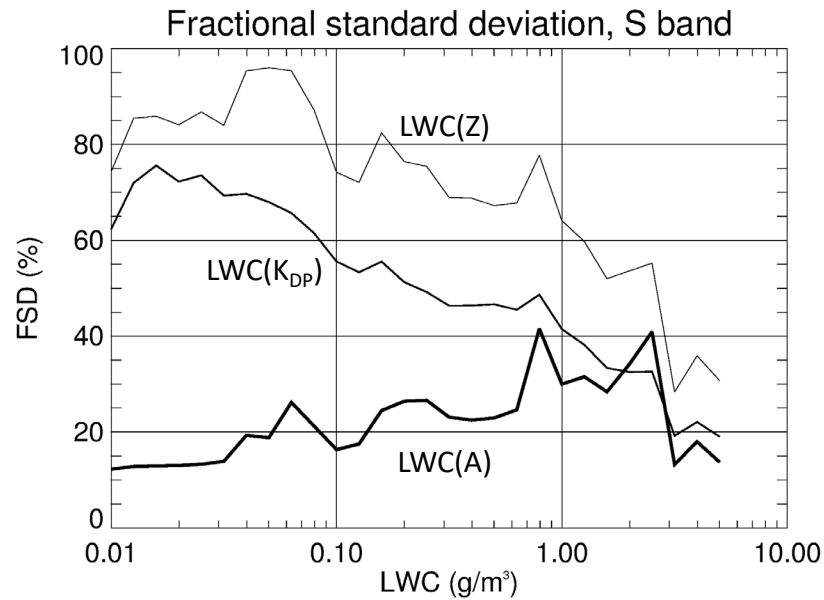


# Estimation of rain rate (R) S band



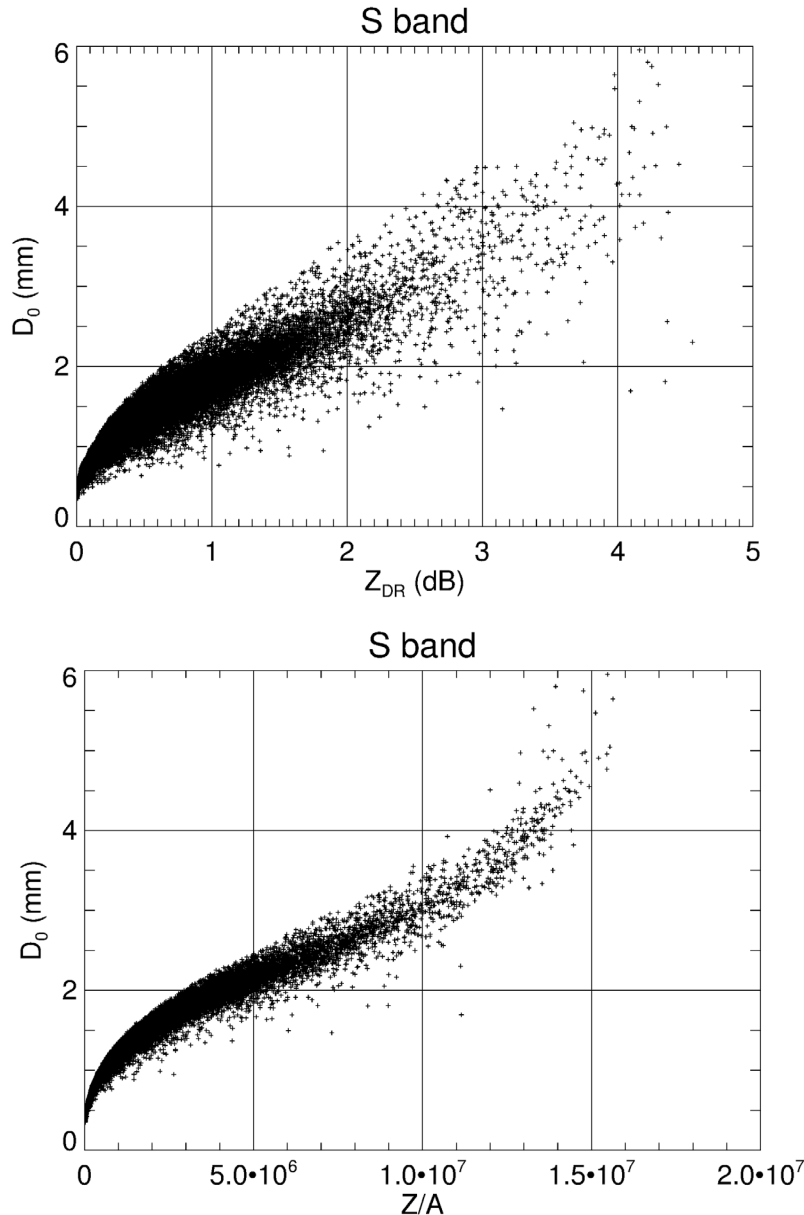
- The estimates of LWC and R from specific attenuation A are much less affected by the DSD variability than the Z- or  $K_{DP}$ -based estimates
- The A-based estimates are immune to radar miscalibration, attenuation, partial beam blockage, and impact of wet radome
- Cloud modeling community should utilize specific attenuation for estimation of LWC and R following its successful use for the WSR-88D QPE. R(A) and LWC(A) can be made a routine products on the WSR-88D network

# Fractional standard deviation of the LWC estimate



- The accuracy of the LWC estimate is a function of LWC varying between 15 and 25% for lower LWC and not exceeding 40% for larger LWC
- The accuracy of the LWC(A) estimator is 4 – 5 times better than the one for the R(Z) estimator for lower LWC

# Estimation of the median diameter of raindrops $D_0$



- Differential reflectivity  $Z_{DR}$  is commonly used for estimation of  $D_0$
- FSD of the estimate related to the DSD variability is 10 – 12 %
- Measurement errors of  $Z_{DR}$  (as low as 0.1 – 0.2 dB) may produce much larger impact on the accuracy of the  $D_0$  estimate than the DSD variability, especially for lower values of  $D_0$
- Combined use  $Z$  and  $A$  may offer a very attractive alternative to the  $Z_{DR}$  – based estimator. This requires further exploration



# **Polarimetric microphysical retrievals in ice / snow**

# Ice microphysical retrievals

- All existing ice microphysical retrievals are based on the use of radar reflectivity  $Z$  measured at a single or multiple radar frequencies
- The  $IWC(Z)$  relations are notoriously inaccurate because they are strongly parameterized by (a) mass-weighted diameter  $D_m$ , (b) total concentration  $N_t$ , and (c) density (or degree of riming)

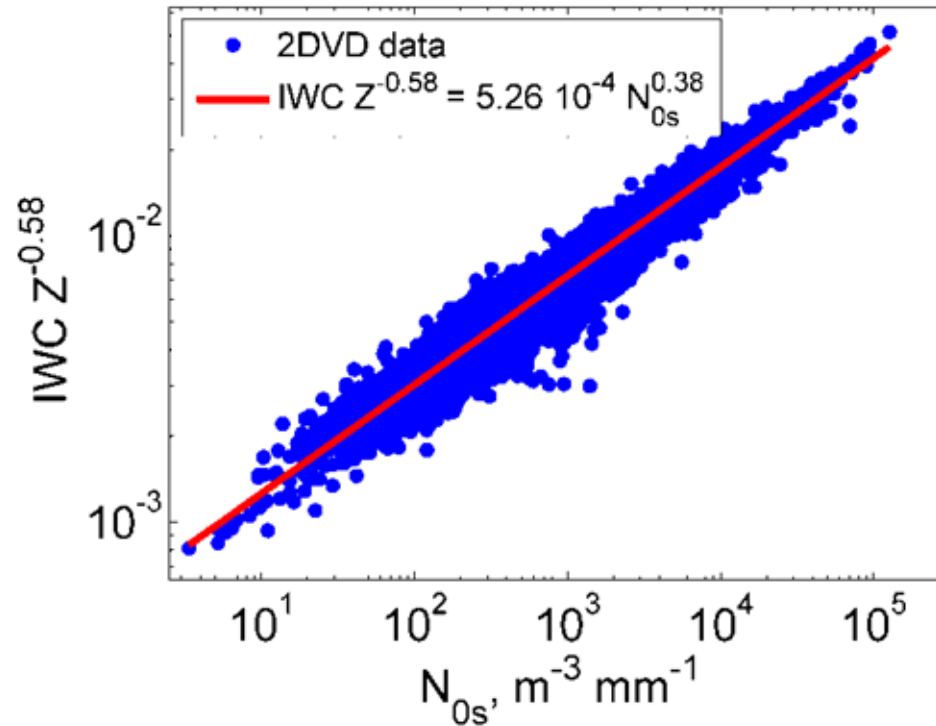
$$N(D) = N_{0s} \exp(-\Lambda_s D) \quad \rho(D) = \alpha D^{-1} \quad \Lambda_s = 4 / D_m$$

$$IWC = 3.81 10^{-4} \alpha^{-0.2} N_{0s}^{0.4} Z^{0.6} \quad IWC = 3.09 10^{-3} \frac{Z}{\alpha D_m^2}$$

- $D_m$  varies 2 orders of magnitude
- $N_t$  varies 4 orders of magnitude
- $\alpha$  changes at least by a factor of 4

# Variability of the intercept in the IWC(Z) power-law relation as a function of $N_{0s}$ (Bukovcic et al. 2018)

Disdrometer snow measurements in Oklahoma



# Basic formulas for polarimetric ice retrievals

$$Z = \frac{|K_i|^2}{|K_w|^2} \frac{1}{\rho_i^2} \int \rho_s^2(D) D^6 N(D) dD$$

$$K_{DP} = \frac{0.27\pi}{\lambda \rho_i^2} \left( \frac{\epsilon_i - 1}{\epsilon_i + 2} \right)^2 \int F_{shape} F_{orient} \rho_s^2(D) D^3 N(D) dD$$

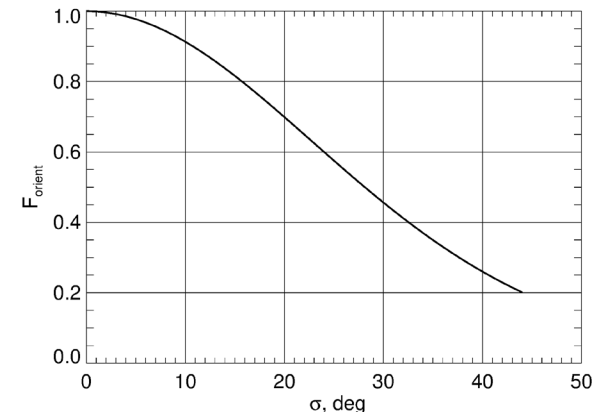
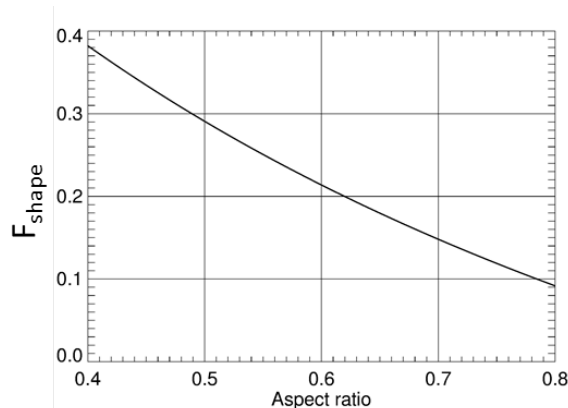
***Z is proportional to the 4<sup>th</sup> moment of snow SD whereas  
K<sub>DP</sub> is proportional to its 1<sup>st</sup> moment***

## Exponential size distribution

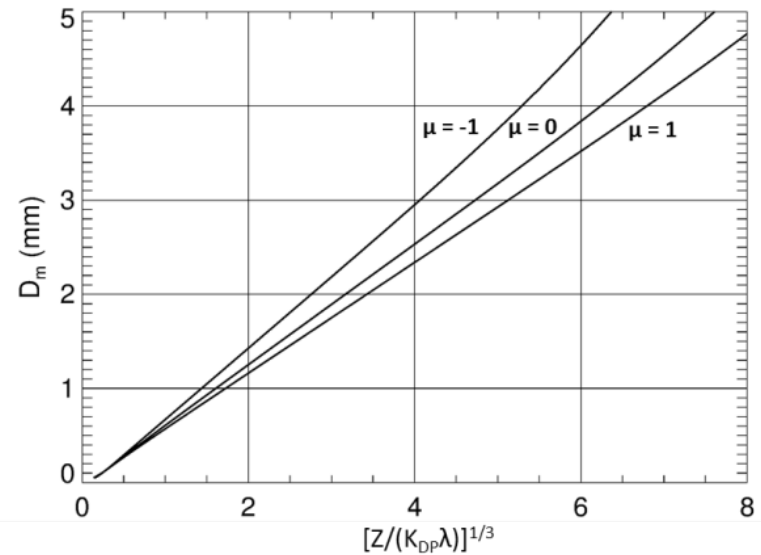
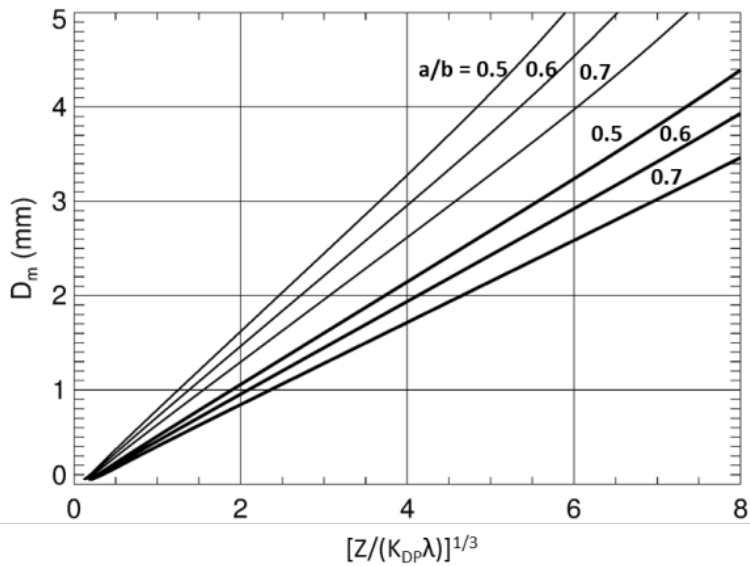
$$Z = 5.30 \cdot 10^{-3} \alpha^2 N_{0s} D_m^5$$

$$K_{DP} = 1.02 \cdot 10^{-2} F_{shape} F_{orient} \frac{\alpha^2 N_{0s}}{\lambda} D_m^2$$

$$\frac{Z}{K_{DP} \lambda} = 0.520 \frac{D_m^3}{F_{shape} F_{orient}}$$



# Median volume diameter as a function of $[Z/(K_{DP}\lambda)]^{1/3}$



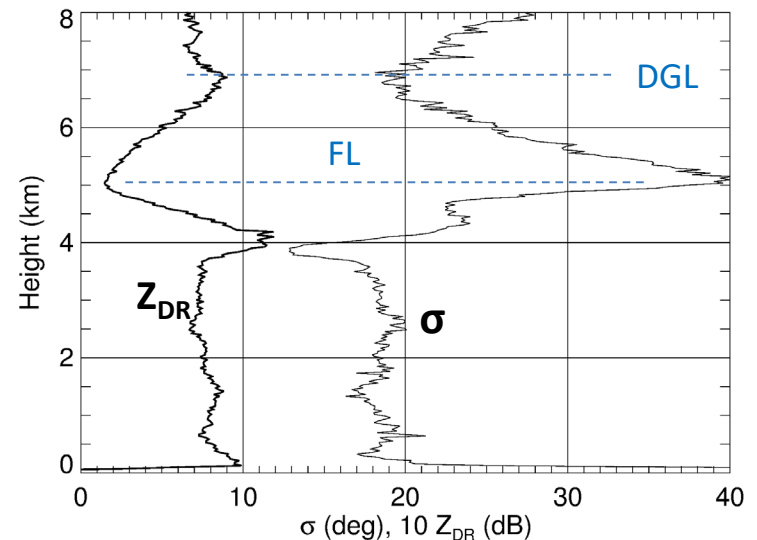
Thin lines –  $\sigma = 10^\circ$

Thick lines –  $\sigma = 40^\circ$

$$\sigma = \frac{180}{\pi} \frac{L_{dr}^{1/2}}{(1 + Z_{dr}^{-1} - 2\rho_{hv} Z_{dr}^{-1/2})^{1/2}}$$

The width of the canting angle distribution  $\sigma$  in ice typically varies between 10 and 40°. This is a serious source of uncertainty

## Radar-retrieved vertical profile of $\sigma$

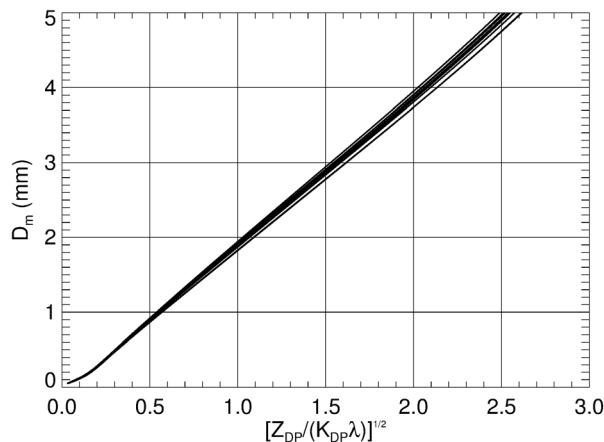


# Utilization of the $Z_{DP}/K_{DP}$ ratio for estimation of $D_m$

$$Z_{DP} = Z_h - Z_v$$

$$h = cL^d$$

Crystal habit	c	d
1. Dendrites	0.038	0.377
1. Solid thick plate	0.230	0.778
1. Hexagonal plates	0.047	0.474
1. Solid columns (L/h < 2)	0.637	0.958
1. Solid columns (L/h > 2)	0.308	0.927
1. Hollow columns (L/h < 2)	0.541	0.892
1. Hollow columns (L/h > 2)	0.309	0.930
1. Long solid columns	0.128	0.437
1. Solid bullets (L < 0.3 mm)	0.250	0.786
1. Hollow bullets (L > 0.3 mm)	0.185	0.532
1. Elementary needles	0.073	0.611



$$D_m = -0.1 + 2.0\eta \quad \eta = \left( \frac{Z_{DP}}{K_{DP}\lambda} \right)^{1/2}$$

$$\gamma = \alpha D_m^2 \approx 0.78\eta^2 = 0.78 \frac{Z_{DP}}{K_{DP}\lambda}$$

$$\log(N_t) = 0.1Z(\text{dBZ}) - 2\log(\gamma) - 1.33$$

$$IWC \approx 4.010^{-2} \frac{K_{DP}\lambda}{1 - Z_{dr}^{-1}}$$

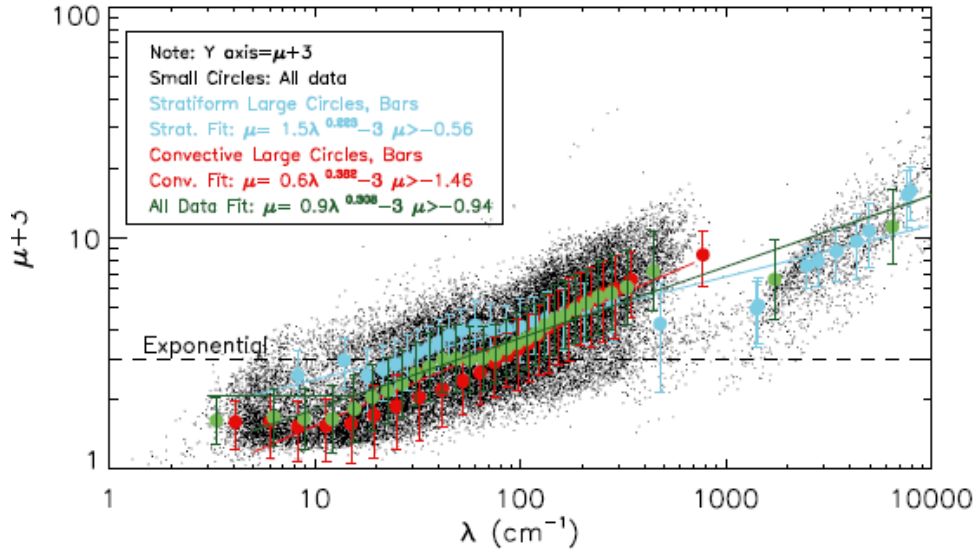
The  $Z_{DP}/K_{DP}$  ratio provides estimate of  $D_m$  which is immune to the particles shape and orientation

# Sensitivity to the microphysical variability of ice hydrometeors

- The suggested estimates of IWC and  $D_m$  are not sensitive to the variability of number concentration
- The suggested relations have been optimized for exponential size distribution of ice, hence they may need to be adjusted for gamma SD (particularly for negative shape factor  $\mu$ ).
- The FSD of the IWC and  $D_m$  estimates is within 20 % if  $-1 < \mu < 1$
- IWC tends to be overestimated and  $D_m$  - underestimated for  $\mu < -1$
- The  $D_m(K_{DP}, Z)$  estimate is immune to the variations of ice density (or  $m - D$  relations) but is sensitive to the shape and orientations of ice particles
- The  $D_m(K_{DP}, Z_{DP})$  relation is immune to the variability of shapes and orientations but is sensitive to ice density (or degree of riming).

# General dependencies of the shape factor $\mu$

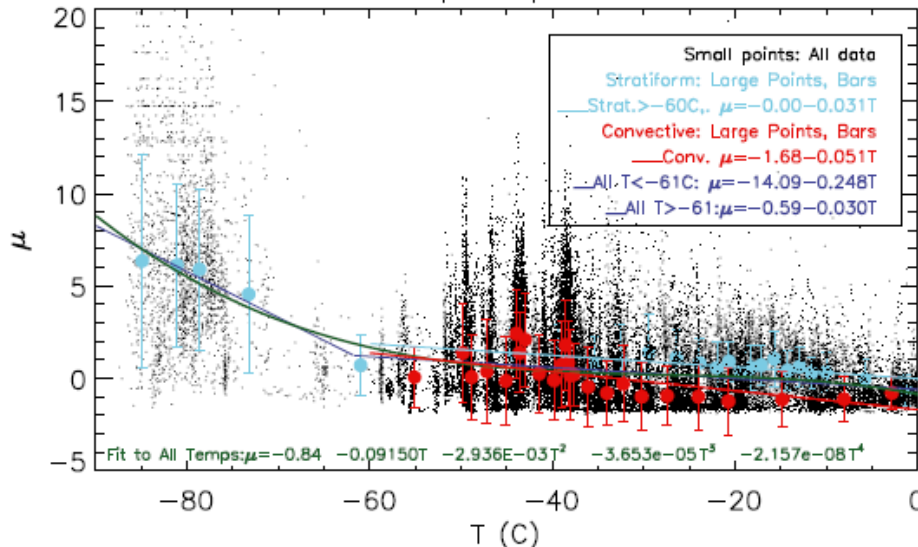
PSD Dispersion  
a:  $\lambda$  Dependence



Heymsfield et al. 2013

- Factor  $\mu$  tends to be negative as a result of aggregation
- Average factor  $\mu$  is close to 0 (exponential SD) within the DGL

b: Temp. Dependence

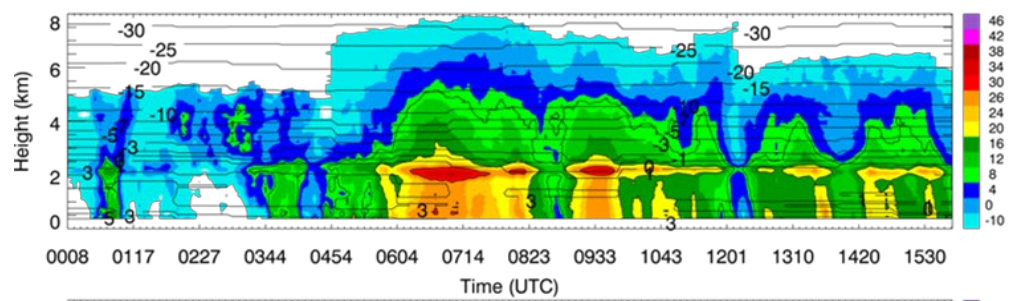




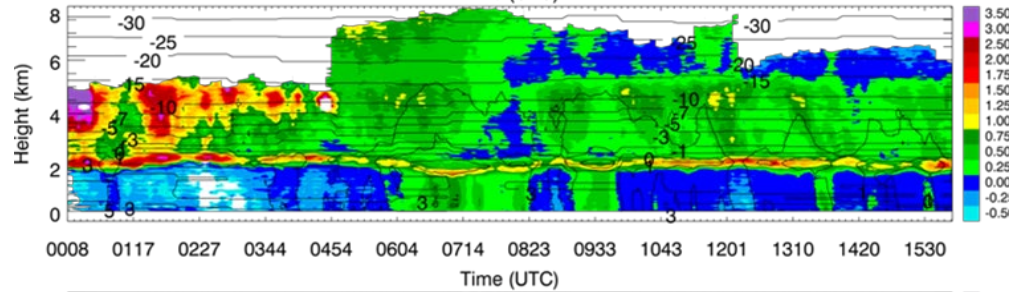
## The impact of measurements errors of $K_{DP}$ and $Z_{DR}$ ( $Z_{DP}$ )

- Statistical errors of the point measurements of  $K_{DP}$  and  $Z_{DR}$  are prohibitively large.  $SD(D_m) > 70\%$  if  $K_{DP} < 0.05$  deg/km;  $SD(D_m) > 25\%$  if  $Z_{DR} < 0.2$  dB
- Aggressive spatial averaging of  $K_{DP}$  and  $Z_{DR}$  is required to obtain their meaningful values which inevitably results in the degradation of spatial resolution
- Various techniques for processing and presentation of polarimetric radar data have been developed recently (QVP, range-defined QVP, CVP, 4D-grid) to reveal polarimetric signatures in ice / snow, to reduce statistical errors in polarimetric radar variables, and improve their vertical resolution
- The best results are achieved in the dendritic growth layer and the worst are just above the freezing level where  $K_{DP}$  and  $Z_{DR}$  signatures almost vanish as a result of strong aggregation of dry snowflakes

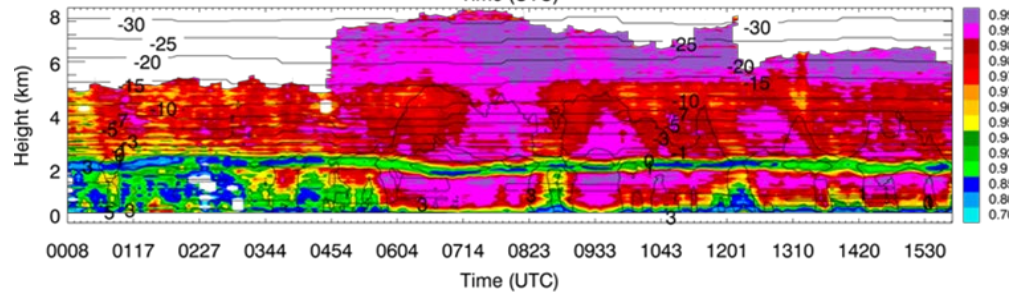
# QVP example for stratiform rain



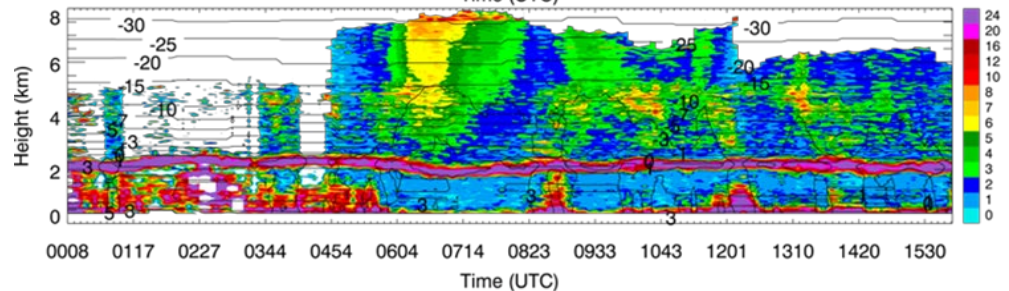
Z



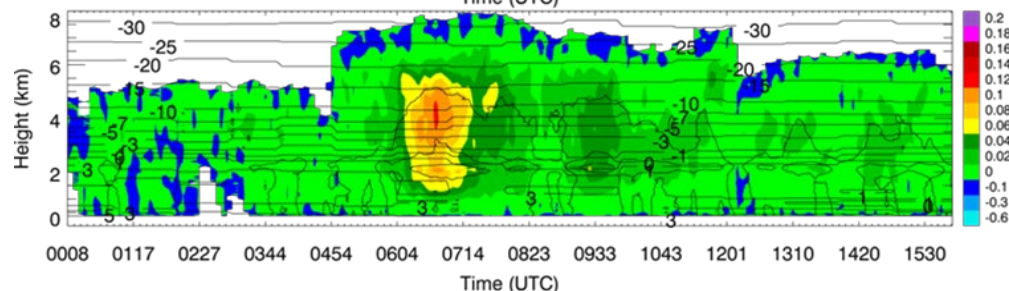
Z<sub>DR</sub>



$\rho_{hv}$



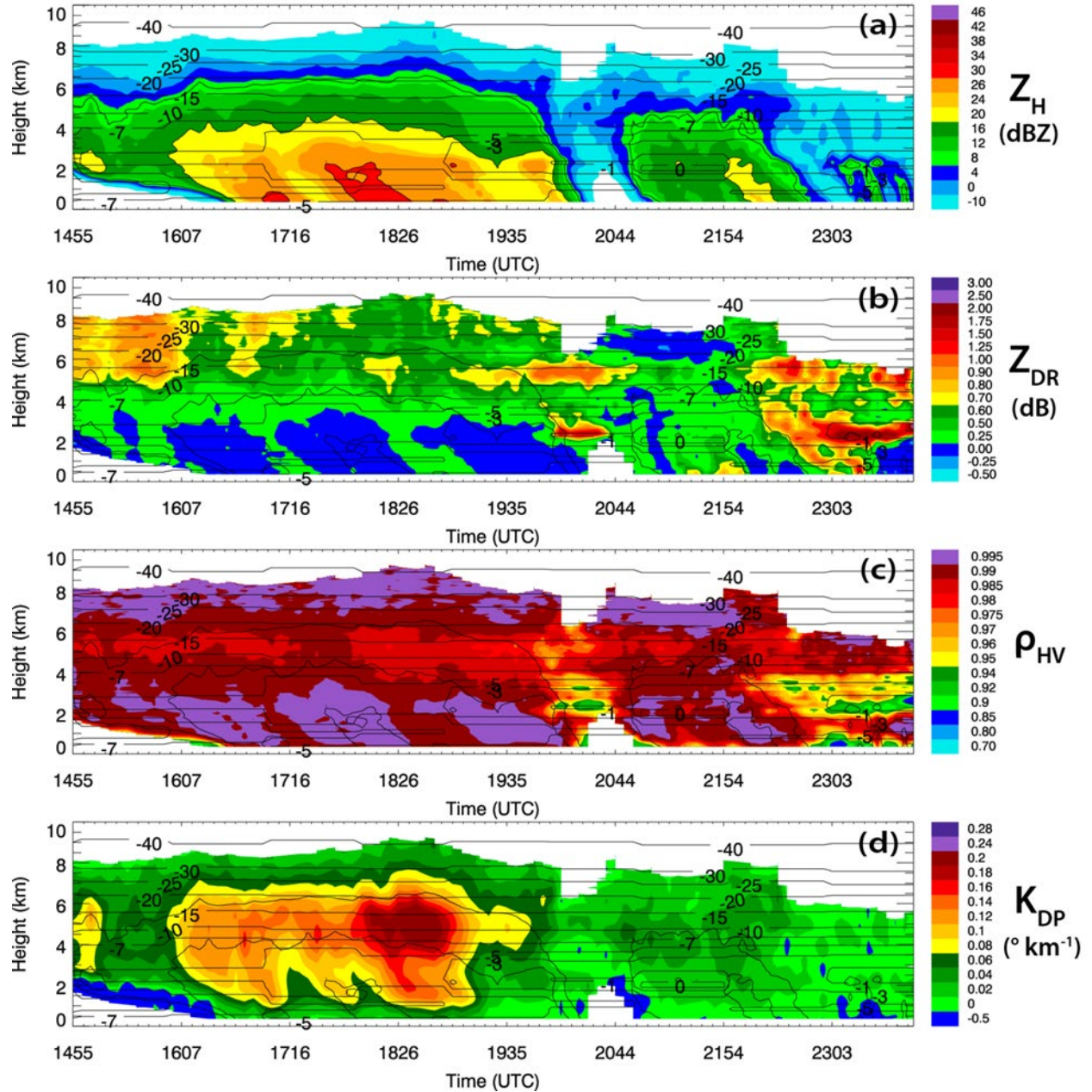
$\Phi_{DP}$



K<sub>DP</sub>

# QVP example for snow

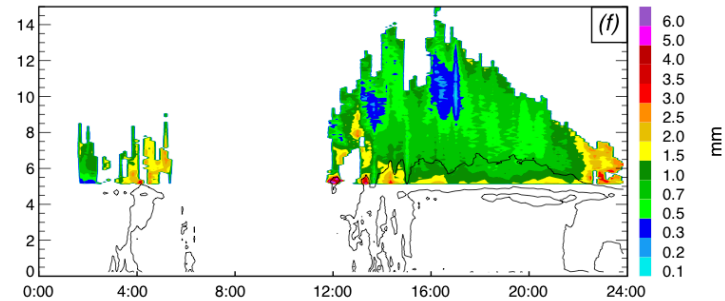
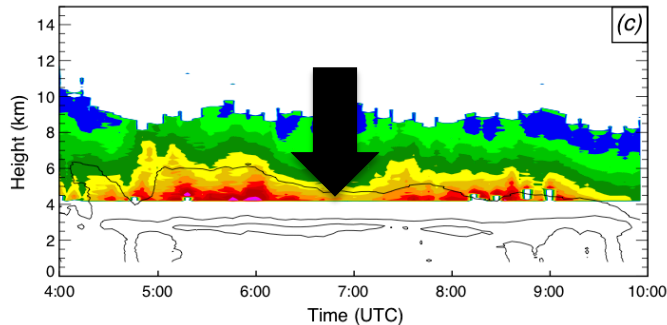
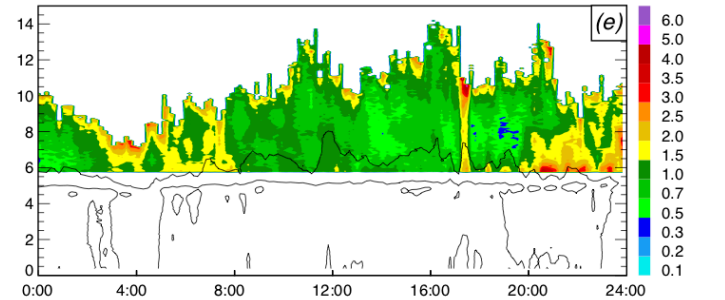
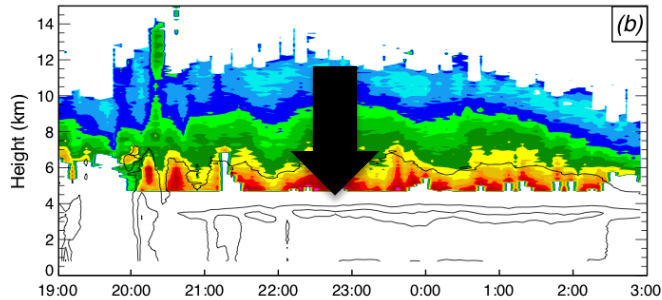
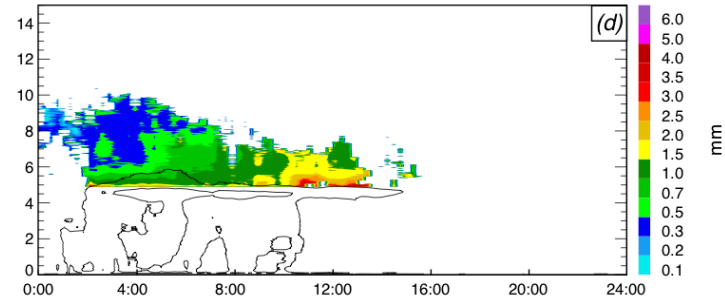
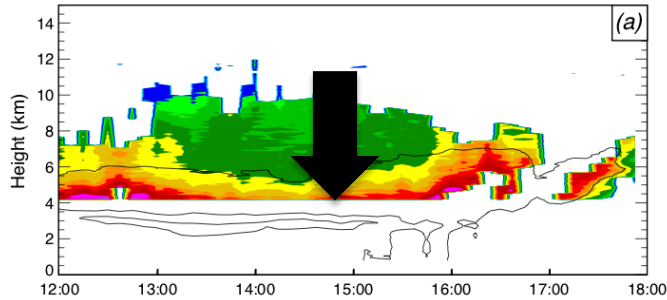
KDIX 9.9°  
8 Dec 2013



# Midlatitude vs. Tropical MCSs

$D_m$ : Midlatitude

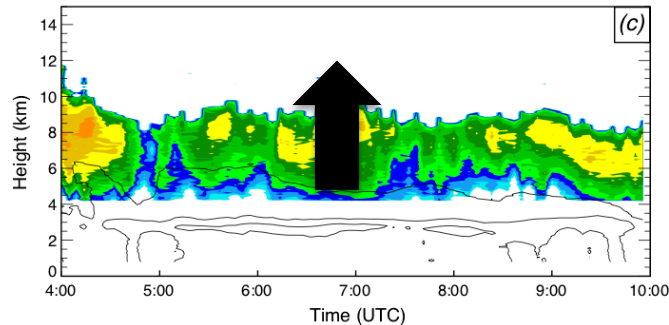
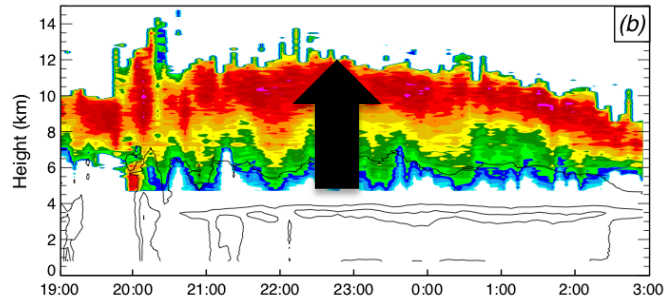
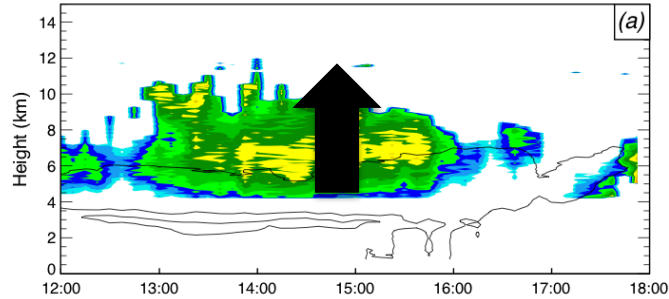
$D_m$ : Tropical



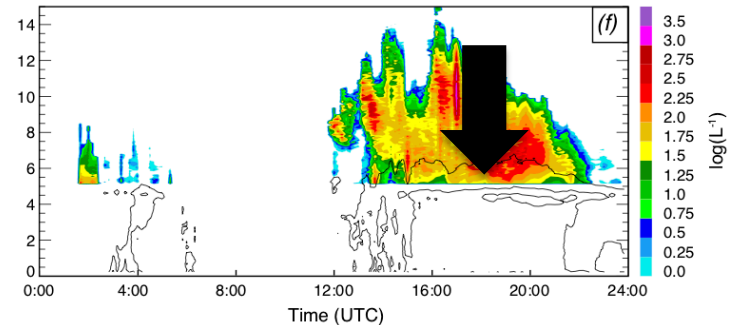
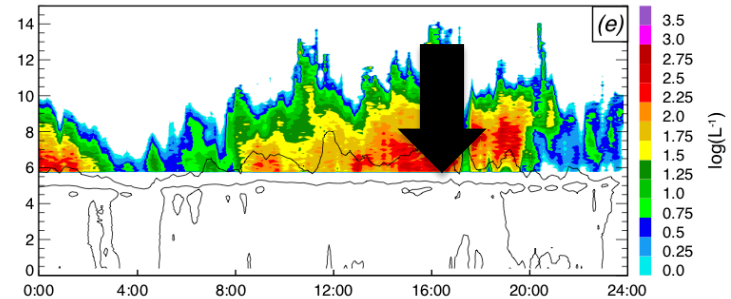
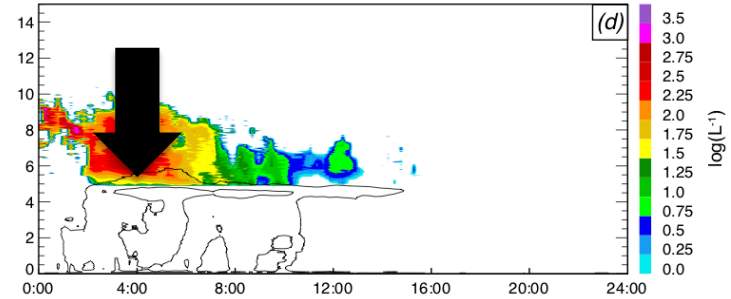


# Midlatitude vs. Tropical MCSs

$\log(N_t)$ : Midlatitude

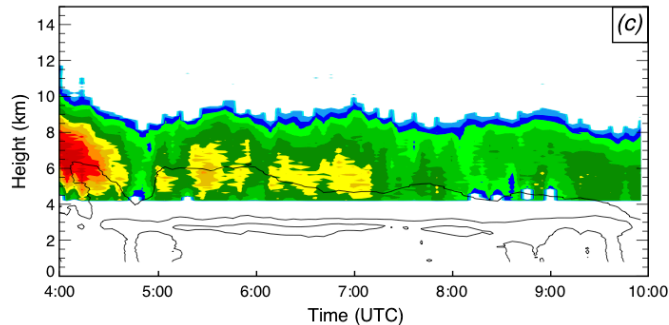
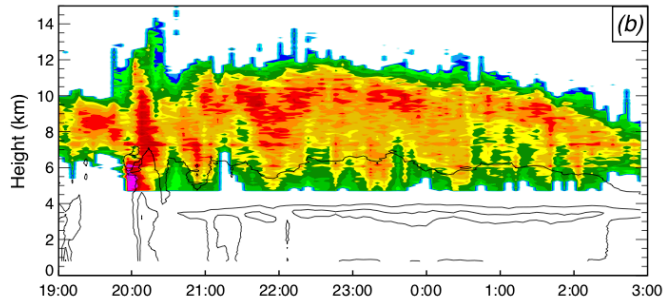
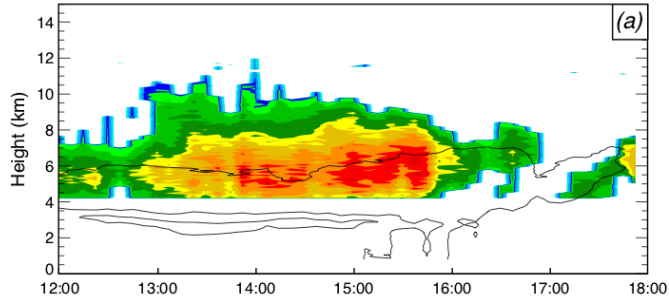


$\log(N_t)$ : Tropical

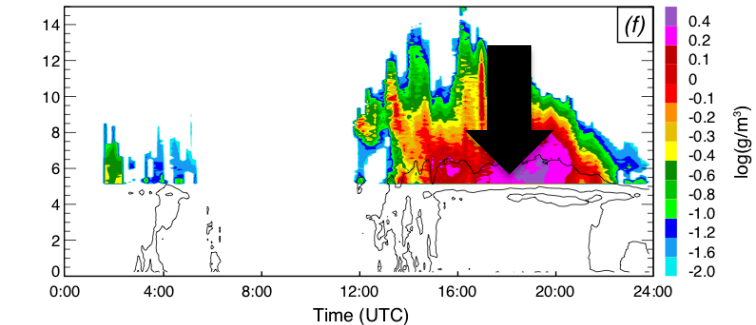
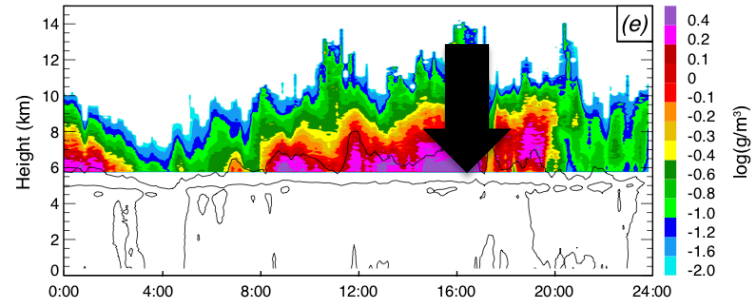
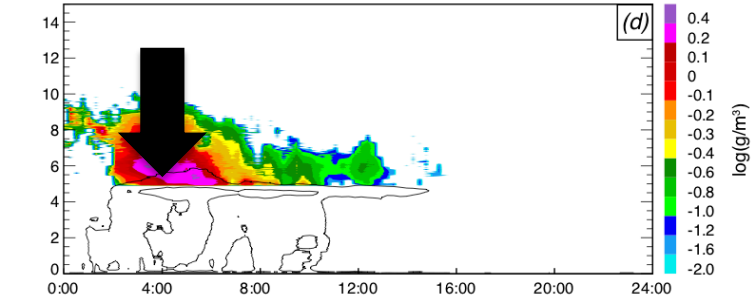


# Midlatitude vs. Tropical MCSs

log(IWC): Midlatitude



log(IWC): Tropical



# Dual-frequency polarimetric radar measurements with Ka-band and S-band radars

*Courtesy of Pavlos Kollias and Mariko Oue*

**KASPR**

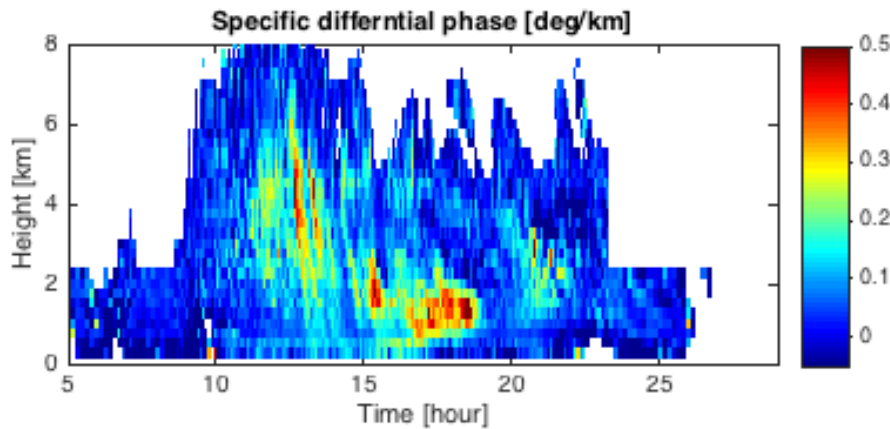
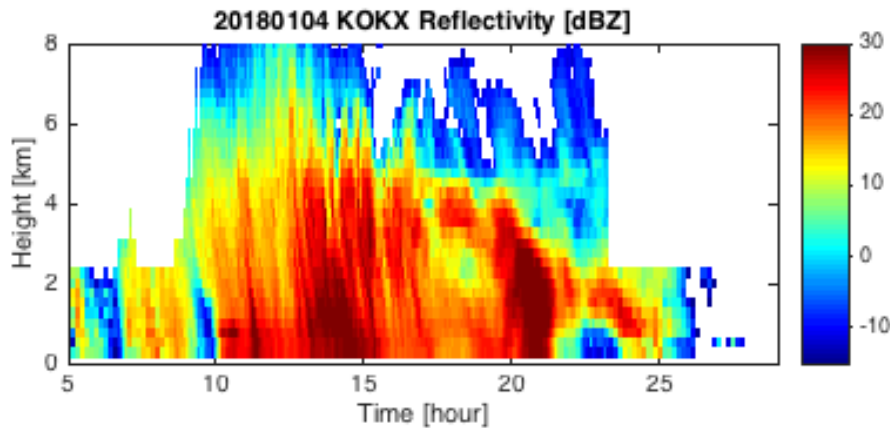
**WSR-88D**



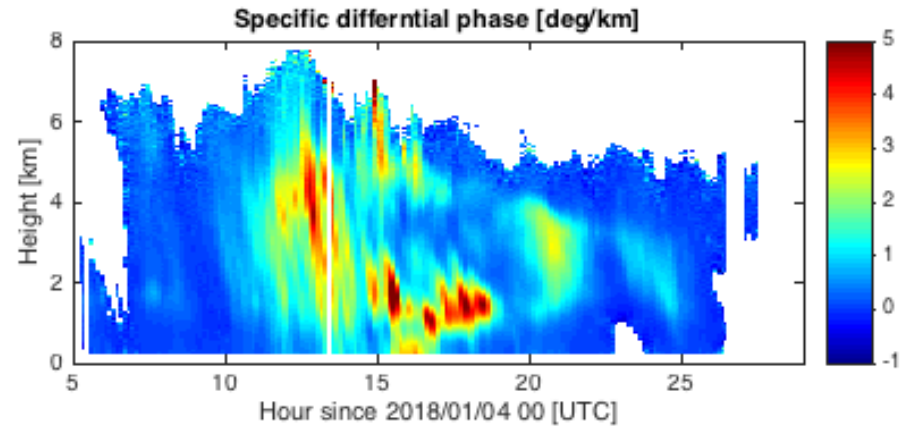
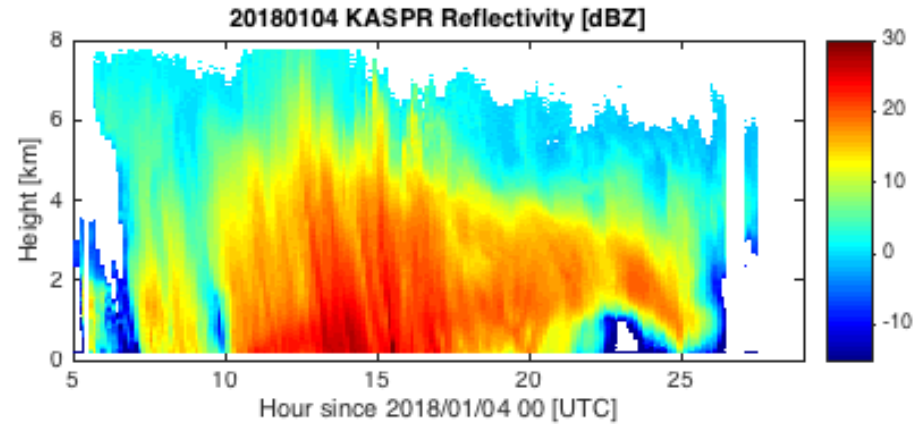
**SBU – Stony Brook University**

**KASPR – Ka-band scanning polarimetric radar**

## KOKX WSR-88D



## KASPR

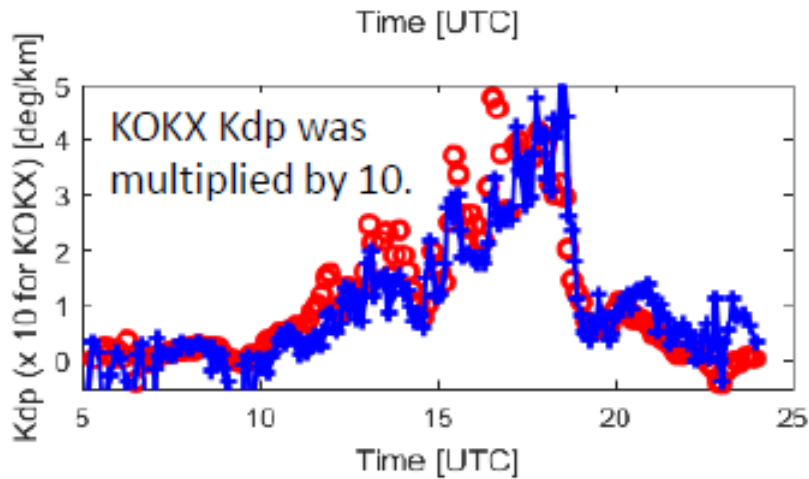


KOKX and KASPR Kdps are almost perfectly matched

The difference between  $Z(Ka)$  and  $Z(S)$  are related to (1) resonance scattering, (2) attenuation, and (3) differences in sensitivities and sampling volumes

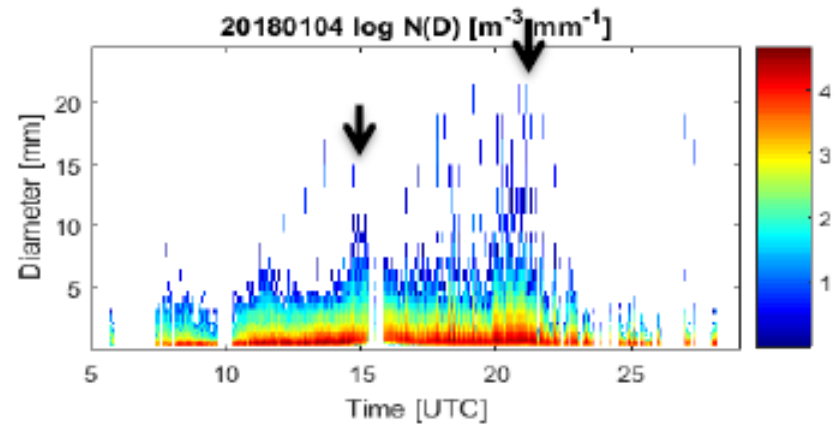
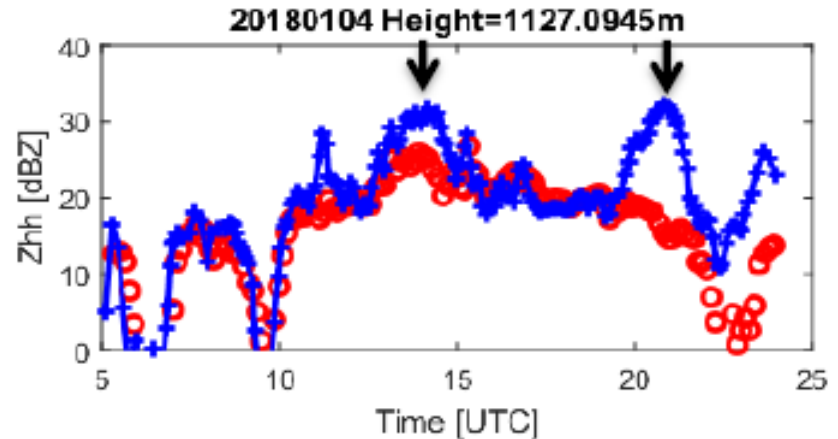


## Comparison of Z and Kdp measured by KASPR and KOKX at 1 km altitude



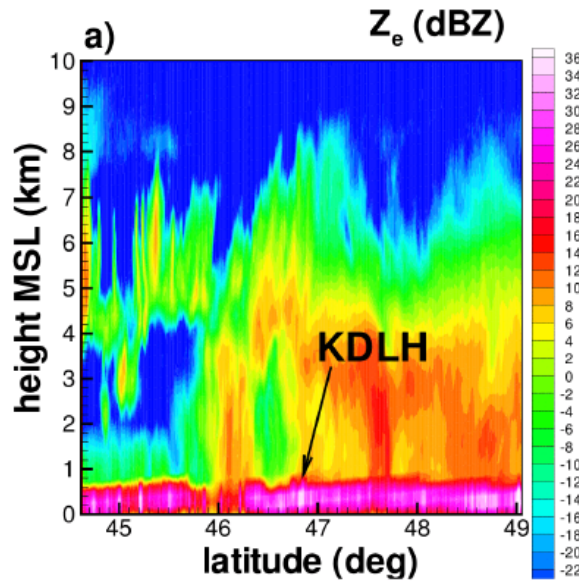
-+- KOKX  
-o- KASPR

The dual-wavelength ratio is high when large snow aggregates are measured by the Parsivel disdrometer - Mie scattering

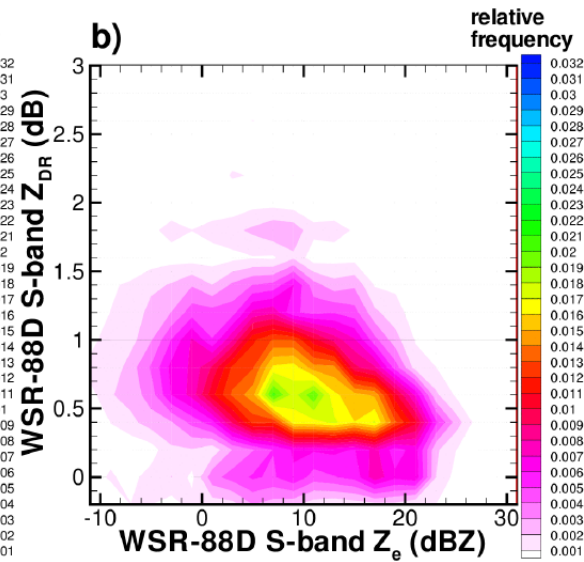
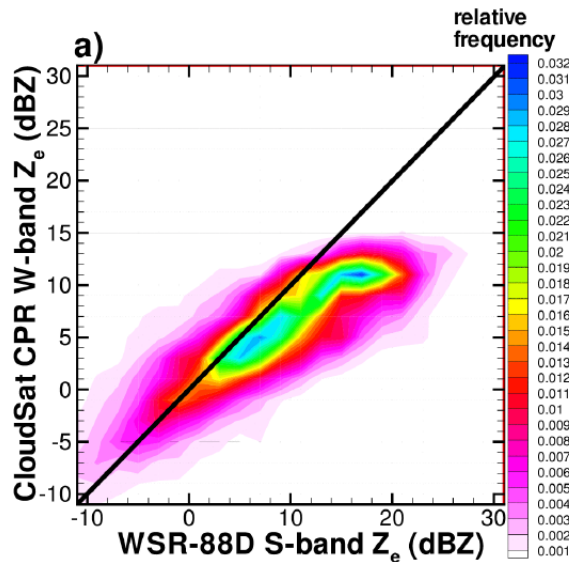
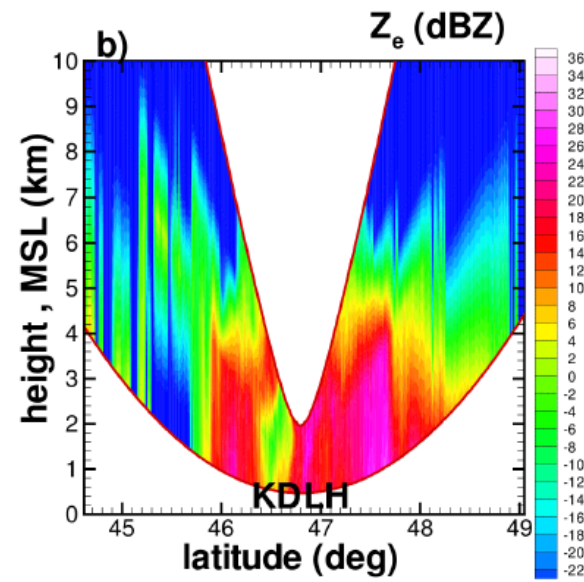


# Dual-frequency polarimetric radar measurements from satellite and ground-based radars (Matrosov 2018)

CloudSat  
W band



WSR-88D  
S band



# Conclusions

- The quality of microphysical retrievals can be significantly improved if multiparameter (particularly polarimetric) radar measurements are used instead of a sole reflectivity factor
- It is strongly recommended to use specific attenuation  $A$  for microphysical retrievals in rain
- Novel polarimetric algorithms for microphysical retrievals in ice / snow show great promise and outperform conventional techniques based on reflectivity
- Recently developed techniques for processing and displaying polarimetric radar variables (e.g., QVP) allow to recognize “fingerprints” of individual microphysical processes and to improve the quality of radar estimates and retrievals
- The network of WSR-88D radars provides tremendous resource for cloud modelers, particularly if complemented with higher-frequency cloud radars operated on the ground or from space